

## Class 6

### Dynamic Randomness: The Poisson Process (Scaling and Centering of Data (Statistical Regularity))

#### Dynamic Randomness: the Poisson Process

- Empirical Introduction, via DataMOCCA.
- The Poisson Process: 4 Definitions, Properties.
  - PASTA = Poisson Arrivals See Time Averages.
  - Biased Sampling.
- Animation: from Bernoulli to Poisson, or The Law of Rare Events.
- Non-homogeneous Poisson Processes.
- Testing: Poisson or not Poisson.
- Modeling Arrivals to a Service Station.
- Forecasting of the Arrival Rate.
- Beyond Poisson: eg. Internet Applications.

#### Scaling and Centering of Data, within the framework of Levy Processes

- Random Walks: leading to Brownian Motions (CLT), Poisson Processes (Rare Events).
- The Invariance Principle (Donsker's Theorem).
- Mathematical Framework: Levy Processes;  
The Axiomatic Approach (Poisson, Compound Poisson, Brownian Motion).
- Beyond second moments: Stable Processes.

#### Recitation 6: SEEStat.

**HW 6:**, “SEEStat”.